



2

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- Numbers and how they are represented in the cognitive system
- Numerical experiences are shaped by culture
 - Reading habits
 Cognitive psychology perspective
 - Educational systems
 - Intensity of training/learning strategies (extra study slide)
 - Spoken language differencesWritten language differences

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Ethno-mathematics

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Part 1: Learning outcomes

- 1. Define the term numerosity
- 2. Present evidence in support of the view that numbers are represented on a mental number line
- 3. Evaluate how reading habits may influence numerical cognition
- 4. To describe cultural influences on arithmetic taskinduced changes in brain (extra study slide)

4

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An everyday essential....

- Doublechecking what room I am teaching in
- Ordering one coffee and paying the exact price
- Getting the right bus number
- Printing the correct number of handouts
- Checking what the time to have a 15 minute break





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Numerosity

- 'How many things in a set'
- Understanding this concept involves understanding:
 - Sets of things (not necessarily visible) have numerosities
 Numerosities can be altered by combining/removing subsets
 - etc
 - One-to-one principle: Two sets have the same numerosity if and only if members of each can be put in 1-to-1 correspondence with none left over
 - Magnitudes are different to numerical orders ("he came first") and semantic labels (call "999")

7

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- The study of how humans (and nonhumans) perceive, represent and compute quantities
- An impressive human achievement
- A fairy recent human achievement (Ifrah, 1998)



8

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How are numbers represented?

- Key characteristics of our mental representations of numerosity (e.g., extracted from arrays of visually presented objects)
- Insights from relevant methodologies
- 1. Counting experiments
- 2. Comparison experiments

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- Easy!
- But gets harder after 4...
- Differences in numerical abilities for numbers within the subitizing range (up to 4) and numbers above the special number 4 (counting range)

17



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- · Possible to get it right without needing to actually count the dots
- Response speed depends on a) whether numerosity is correlated with other continuous quantities (e.g. how much space the dots take on a screen)
- · Response speed depends on a) the ratio of the difference (e.g. 1:4 harder than 1:10 ratio) • This is called "Weber's law"

23

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To sum up....

- · We are able to extract both exact and approximate numerosities using two different cognitive systems (e.g. dissociated in patients with acalculia)
- 1. Exact system
 - Subitizing range: fixed upper limit ('4')
 - Numbers above 4 are counted at a processing time cost that is linearly related to the set size
- 2. Approximate system (has no size limit) but represents numbers only approximately
- Subject to Weber's law: our sensitivity to changes in numerosity depends on the discriminability ratio

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A third system?

- Underlying the use of quantifiers, number words, and verbal counting
 - Link with language (thus, most likely to be affected by culture)
 - Arabic numerals: "Which one is bigger, 8 or 5?"
- Much evidence to suggest that the cognitive interpretation of number symbols links back to the quantities they represent.
 - E.g., shorter time needed to compare numbers 'further apart' (8 vs 1 relative to 8 vs 7) (distance effect). This has been taken to suggest that we represent numbers spatially in a number line

25

The Mental Number Line (MNL)



- Close your eyes and imagine the number the numerical sequence 1-30. What do you see?
- When asked to think about numbers, people often activate a mental number line (MNL), oriented left to right
- Early illustrations of number lines date back at least to the late 17th century (Galton, 1881; The Visions of Sane Persons)

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Is this mental number line characteristic shared universally across cultures?